Name: $\qquad$
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## 15-121 Fall 2019 Quiz 10

Up to 25 minutes. No calculators, no notes, no books, no computers. Show your work!

## 1. Binary Search Tree

Consider the following code for a binary search tree of integers. (There is nothing special here, the code is provided just in case you forgot how a binary tree is built.)

```
public class BinarySearchTree {
    private TreeNode root;
    private class TreeNode {
        private int data;
        private TreeNode left;
        private TreeNode right;
        private TreeNode(int data) {
            this.data = data;
        }
    }
    public BinarySearchTree() {
        root = null;
    }
    public void add(int item) {
        root = add(root, item);
    }
    private TreeNode add(TreeNode root, int item) {
        if (root == null) {
            return new TreeNode(item);
    }
    if (item < root.data) {
        root.left = add(root.left, item);
    } else {
            root.right = add(root.right, item);
        }
        return root;
    }
}
```

(a) (5 points) Write the code for a new method in this class called largest(), which returns the value of the largest integer in the tree. Your method must be $O(\log N)$. If the tree is empty, return -1 .
(b) (7 points) Write the code for a new method in this class called sum(), which returns the sum of all the integers in the tree. You may also write any additional helper methods that you need. Your method must be $O(N)$. Hint: You should do this recursively.
(c) (8 points) Write the code for a new method in this class called height(), which returns the height of the tree. You may also write any additional helper methods that you need. Your method must be $O(N)$. Hint: You should do this recursively. Also, this is the same as the homework.

